Putnam Mathematical

Competition

The 2018 Putnam Mathematical Competition will take place on **Saturday, December 1** at 9AM in MSCS 514. This national problem-solving competition is open and free to any OSU undergraduate who registers at MSCS 401 before **Friday, Oct. 12**. Prizes and glory are available. You can also register by emailing

dosev@okstate.edu or wrightd@okstate.edu.

Past problems from the competition:

1. Given a positive integer *n*, what is the largest *k* such that the numbers 1, 2, ..., *n* can be put in *k* boxes so that the sum of the numbers in each box is the same?

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[When n = 8, the example \{1, 2, 3, 6\}, \{4, 8\}, \{5, 7\} shows that the largest k is at least 3.]
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- 2. Let S be the smallest set of positive integers such that
 - a) 2 is in S,
 - b) n is in S whenever n^2 is in S, and
 - c) $(n+5)^2$ is in S whenever n is in S.

Which positive integers are not in *S*? (The set *S* is "smallest" in the sense that *S* is contained in any other such set.)

- 3. Let L_1 and L_2 be distinct lines in the plane. Prove that L_1 and L_2 intersect if and only if, for every real number $\lambda \neq 0$ and every point P not on L_1 or L_2 , there exist points A_1 on L_1 and A_2 on L_2 such that $\overrightarrow{PA_2} = \lambda \overrightarrow{PA_1}$.
- 4. Let $a_0 = 1$, $a_1 = 2$, and $a_n = 4a_{n-1} a_{n-2}$ for $n \ge 2$. Find an odd prime factor of a_{2015} .

Later in the fall semester, we will email interested students about meetings where we discuss problem-solving strategies.